

# Numerical Codes for Electron Cyclotron heating and Current Drive

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## TORAY-FOM ray-tracing code

Code status: 'on ITM-Gateway'  
Solves 3D geometric optics ray-tracing equations

$$\frac{d\mathbf{r}}{dt} \equiv \mathbf{v}_{gr} = \frac{\partial \Omega}{\partial \mathbf{k}} = -\frac{\partial D/\partial \mathbf{k}}{\partial D/\partial \omega} \quad \frac{d\mathbf{k}}{dt} = -\frac{\partial \Omega}{\partial \mathbf{r}} = \frac{\partial D/\partial \mathbf{r}}{\partial D/\partial \omega}$$

Gaussian wave beam modeled with rectangular grid of rays.

Options for cold or warm (weakly and fully relativistic) ray-trajectories.

## Equilibrium: provides a choice of

Analytic circular magnetic equilibrium including Shafranov shift

2D equilibria from bi-cubic spline fits to EQDSK data

Density and temperature profiles either analytic form or from cubic spline fit to data

option to include a magnetic island

## Power absorption (choice of)

Weakly relativistic (1<sup>st</sup> and 2<sup>nd</sup> harmonic lowest order FLR)

Fully relativistic (arbitrary range of harmonics and of terms in FLR expansion)

## Adjoint Current Drive calculation (choice of)

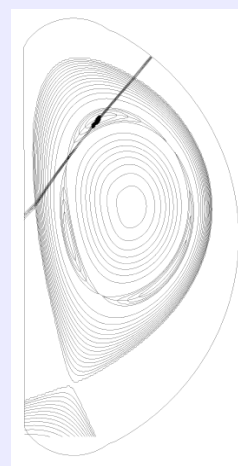
Cohen R.H. 1987 *Phys. Fluids* 30 2442

Lin-Liu Y.R. et al. 2003 *Phys. Plasmas* 10 4064

## ITER scenario 2

Lower Steering Mirror

3/2 mode



## RELAX bounce averaged Fokker-Planck code

Code status: 'on ITM-Gateway'  
Solves 2D velocity + 1D real space Fokker-Planck equation

$$\frac{\partial f_e}{\partial t} = \left\langle \sum_s C(f_e, f_s) \right\rangle_{\phi_B} - \left\langle \langle \hat{r}_{q1} \rangle_{\phi} \right\rangle_{\phi_B} - \left\langle q_e \hat{E} \cdot \hat{b} \frac{\partial f_e}{\partial p_{\parallel}} \right\rangle_{\phi_B}$$

General equilibria from spline fits to EQDSK data

## Quasi-linear EC diffusion operator

Gaussian wave beam modeled with grid of rays (obtained from ray- or beam-tracing codes).

$$D_{\mu\mu} = \frac{\pi e^2}{m_e^2 \omega} \frac{\gamma p_{\perp}^2}{B^2} |\bar{G}_{\perp}|^2 \frac{e^{-(\gamma - n\omega_c/\omega - N_{\parallel} x_{\parallel})^2/\Delta Q}}{\sqrt{\pi \Delta Q}} \times \frac{P_0 e^{-\int \alpha ds}}{\Pi \cos \chi} \frac{B}{2\pi \tau_B v_{\parallel} R B_p}$$

Warm, Maxwellian plasma or fully consistent wave polarization.

## Collision operator (choice of)

(relativistic) Maxwellian back-ground

Publications: Peeters A.G., et al. 1995 *PPCF* 37 525

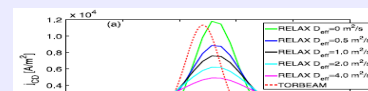
e-i collisions only in pitch-angle scattering Phys. Commun. 9 Additional Physics et al. 2009 *Nucl. Fusion* 49 095018

e-e momentum conserving correction

Isotropic background (energy conserving)

## ITER scen 2

LSM 3/2 mode



Peeters A.G. et al. 1996 *Phys. Plasmas* 3 1628

Radial diffusion

Parallel electric field

Finite orbit width effects: bootstrap current